Algebra 2 Mathematics Item Specifications



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High School Algebra 2 Introduction

In 2014 Missouri legislators passed House Bill 1490, mandating the development of the Missouri Learning Expectations. In April of 2016, these Missouri Learning Expectations were adopted by the State Board of Education. Groups of Missouri educators from across the state collaborated to create the documents necessary to support the implementation of these expectations.

One of the documents developed is the item specification document, which includes all Missouri grade level/course expectations arranged by domains/strands. It defines what could be measured on a variety of assessments. The document serves as the foundation of the assessment development process.

Although teachers may use this document to provide clarity to the expectations, these specifications are intended for summative, benchmark, and large-scale assessment purposes.

Components of the item specifications include:

Expectation Unwrapped breaks down a list of clearly delineated content and skills the students are expected to know and be able to do upon mastery of the Expectation.

Depth of Knowledge (DOK) Ceiling indicates the highest level of cognitive complexity that would typically be assessed on a large scale assessment. The DOK ceiling is not intended to limit the complexity one might reach in classroom instruction.

Item Format indicates the types of items used in large scale assessment. For each expectation, the item format specifies the type best suited for that particular expectation.

Text Types suggests a broad list of text types for both literary and informational expectations. This list is not intended to be all inclusive: other text types may be used in the classroom setting. The expectations were written in grade level bands; for this reason, the progression of the expectations relies upon increasing levels of quantitative and qualitative text complexities.

Content Limits/Assessment Boundaries are parameters that item writers should consider when developing a large scale assessment. For example, some expectations should not be assessed on a large scale assessment but are better suited for local assessment.

Sample stems are examples that address the specific elements of each expectation and address varying DOK levels. The sample stems provided in this document—are in no way intended to limit the depth and breadth of possible item stems. The expectation should be assessed in a variety of ways.

Mathematics		A2.NQ.A.1
NQ	Number and Quantity	
Α	Extend and use the relationship between rational exponents and radicals.	
1	Extend the system of powers and roots to include rational exponents.	
	Expectation Unwrapped	DOK Ceiling 2
The st	udent will apply the rules of exponents to expressions that include rational exponents.	Item Format Selected Response
	udent will simplify expressions including constants and variables as bases and using all exponents, including those with integer numerators other than one.	Constructed Response Technology Enhanced
		Sample Stems
Coefficie	Content Limits/Assessment Boundaries at denominators should be limited to natural numbers of ten or less. and the ten the ten of the	Calculator Designation NEUTRAL — a calculator may or may not be available for items

	Mathematics	A2.NQ.A.2
NQ	Number and Quantity	
Α	Extend and use the relationship between rational exponents and radicals.	
2	Create and recognize equivalent expressions involving radical and exponential forms of express	sions.
	Expectation Unwrapped	DOK Ceiling
The stud	lent will be able to convert from radical form to rational exponent form.	2 Item Format
he stud	lent will be able to convert from rational exponent form to radical form.	Selected Response Constructed Response
The stud	lent will recognize that radical form and rational exponent forms are equivalent.	Technology Enhanced
he stud	lent will be able to simplify radical expressions.	Sample Stems
he stud	lent will be able to simplify expressions with rational exponents.	
	Content Limits/Assessment Boundaries	<u>Calculator Designation</u>
	nators should be limited to natural numbers of ten or less.	NEUTRAL – a calculator may or
	ents are to include only negative one thousand to one thousand.	may not be available for items
	e than three distinct variables.	
idices c	on radicals should not exceed five.	

	criboi Aigebra 2	
	Mathematics	A2.NQ.A.3
NQ	Number and Quantity	
Α	Extend and use the relationship between rational exponents and radicals.	
3	Add, subtract, multiply and divide radical expressions.	
	Expectation Unwrapped	DOK Ceiling
		2
The stud	ent will able to perform operations with radical expressions, including those that require simplifying prior to	Item Format
combinin	ng terms.	Selected Response
		Constructed Response
The stud	ent will use conjugates to simplify rational expressions containing radicals in the denominator.	Technology Enhanced
		realifology Elifatices
		Sample Stems
	Content Limits/Assessment Boundaries	<u>Calculator Designation</u>
•	ons should include those that are numeric and algebraic.	NEUTRAL – a calculator may or
	ndices should be no more than five.	may not be available for items
	than two distinct variables.	
Coefficie	nts negative six hundred twenty-five to six hundred twenty-five.	

	Mathematics	A2.NQ.A.4
NQ	Number and Quantity	
Α	Extend and use the relationship between rational exponents and radicals.	
4	Solve equations involving rational exponents and/or radicals and identify situations where	e extraneous solutions may result.
	Expectation Unwrapped	DOK Ceiling
The stud	dent will solve equations involving rational exponents.	2
	and the control of an	<u>Item Format</u>
he stud	dent will solve equations involving radical expressions.	Selected Response Constructed Response
The stud	Nont will about for and identify outropeous solutions	Technology Enhanced
rne stud	dent will check for and identify extraneous solutions.	Sample Stems
		<u>sample stems</u>
	Content Limits/Assessment Boundaries	<u>Calculator Designation</u>
	g polynomials to solve should not exceed degree two.	NEUTRAL – a calculator may or
•	ns may contain one or two radicals.	may not be available for items
:xpressi	ons with rational exponents should be set equal to a constant.	

nigii School Algebra 2		
	Mathematics	A2.NQ.B.5
NQ	Number and Quantity	
В	Use complex numbers.	
5	Represent complex numbers.	
	Expectation Unwrapped	DOK Ceiling
The section		2
The stud	ent will be able to write all numbers in the form, $a+bi$.	<u>Item Format</u>
The stud	ent will be able to identify that a and b are real numbers and i is defined as the square root of -1.	Selected Response
		Constructed Response Technology Enhanced
		Sample Stems
	Content Limits/Assessment Boundaries	Calculator Designation
		NEUTRAL – a calculator may or
		may not be available for items

I light S	chool Algebia 2	
	Mathematics	A2.NQ.B.6
NQ	Number and Quantity	
В	Use complex numbers.	
6	Add, subtract, multiply and divide complex numbers.	
	Expectation Unwrapped	DOK Ceiling
		2
The stud	ent will add and subtract complex numbers with answers given in $a\ +\ bi$ form.	Item Format
The stud	ent will multiply complex numbers with answers given in $a + bi$ form.	Selected Response
The stad	ent will mataply complex numbers with answers given in a 1 bit form.	Constructed Response
The stud	ent will divide complex numbers with answers given in $a+bi$ form, using conjugates to rationalize the	Technology Enhanced
denomir	ator.	Sample Stems
While cir	Content Limits/Assessment Boundaries nplified answers may have fractional a and/or b values, given problems should use integer values for a and b .	<u>Calculator Designation</u> NEUTRAL — a calculator may or
	ultiplying and dividing, limit a and b to values between negative twelve and twelve.	may not be available for items
	and and an an an an a did a to raised detricent negative there and there.	

	Mathematics	A2.NQ.B.7
NQ	Number and Quantity	•
В	Use complex numbers.	
7	Know and apply the Fundamental Theorem of Algebra.	
	Expectation Unwrapped	DOK Ceiling
The stud	ent will recognize that the degree of a polynomial determines the number of solutions (real + imaginary).	2
THE State	ent will redognize that the degree of a polynomial determines the manual of solutions (real villingshally).	Item Format
The stud	ent will understand that complex solutions always occur in pairs.	Selected Response Constructed Response
The stud	ent will understand that factors repeated n times have a multiplicity of n .	Technology Enhanced
THE Stud	ent will understand that factors repeated in times have a multiplicity of in.	Sample Stems
		<u>sample stems</u>
	Content Limits/Assessment Boundaries	<u>Calculator Designation</u>
Polynom	ial equations should contain integer coefficients.	NEUTRAL – a calculator may or
•	a degree of five or less on given polynomial.	may not be available for items

	Mathematics	A2.SSE.A.1
SSE	Seeing Structure in Expressions	
Α	Define and use logarithms.	
1	Develop the definition of logarithms based on properties of exponents.	
exponer	Expectation Unwrapped lent will develop the definition of logarithms, $\log_b y = x$, if and only if $b^x = y$, based on properties of its. lent will be able to convert equations from exponential to logarithmic form.	DOK Ceiling 2 Item Format Selected Response Constructed Response Technology Enhanced
The stuc	lent will be able to convert equations from logarithmic to exponential form.	Sample Stems
Bases sh	Content Limits/Assessment Boundaries ould be greater than zero.	Calculator Designation NEUTRAL — a calculator may or may not be available for items

	Mathematics	A2.SSE.A.2
SSE	Seeing Structure in Expressions	
A	Define and use logarithms	
2	Use the inverse relationship between exponents and logarithms to solve exponential and logarithmic equations	5.
	Expectation Unwrapped	DOK Ceiling
The stud	ent will use the inverse relationship between exponents and logarithms to solve simple exponential equations.	2
The stud	lent will use the inverse relationship between exponents and logarithms to solve simple logarithmic equations.	Item Format Selected Response Constructed Response Technology Enhanced Sample Stems
		$4\log(2x+4) = 8$ $10^2 = 2x + 4$
•	Content Limits/Assessment Boundaries ressions used as exponents should not exceed linear. The ression used in logarithms should not exceed linear $c \log_n(ax + b) = m$, where n or m are integers and c is a size.	Calculator Designation YES – a calculator will be available for items

	Mathematics	A2.SSE.A.3
SSE	Seeing Structure in Expressions	
Α	Define and use logarithms	
3	Use properties of logarithms to solve equations or find equivalent expressions.	
	Expectation Unwrapped	DOK Ceiling
The stude	ent will expand expressions using properties of logarithms.	2 Item Format
The stude	ent will condense expressions using properties of logarithms.	Selected Response Constructed Response
The stude	ent will solve equations using properties of logarithms.	Technology Enhanced
		<u>Sample Stems</u>
	Content Limits/Assessment Boundaries	Calculator Designation
The base	e is greater than zero.	NEUTRAL – a calculator may or
	than three distinct variables in expanding and condensing problems.	may not be available for items
	is should have no more than two terms on one side of the equation and one term on the other side. is should have the same base throughout.	
No more Equation	than three distinct variables in expanding and condensing problems. It is should have no more than two terms on one side of the equation and one term on the other side.	

	Mathematics	A2.SSE.A.4
SSE	Seeing Structure in Expressions	
Α	Define and use logarithms.	
4	Understand why logarithmic scales are used, and use them to solve problems.	
	Expectation Unwrapped	DOK Ceiling
The stud	ent will demonstrate an understanding of applications of the logarithmic scale and apply it in problem solving.	3
	pple: pH scale, Richter scale, sound intensity, light intensity and the musical scale.	Item Format
		Selected Response Constructed Response
Students	will demonstrate an understanding of how logarithmic scales are used to compare quantities.	Technology Enhanced
		Sample Stems
	Content Limits/Assessment Boundaries	Calculator Designation
	is greater than zero.	YES – a calculator will be available
When gi	ving formulas, all variables should be defined.	for items
1		
1		

	Mathematics	A2.REI.A.1
REI	Reasoning with Equations and Inequalities	
Α	Solve equations and inequalities.	
1	Create and solve equations and inequalities, including those that involve absolute value.	
	Expectation Unwrapped	DOK Ceiling 2
The stud	ent will solve exponential equations that do not require logarithms.	Item Format Selected Response
	ent will write an equation or inequality to model a context.	Constructed Response Technology Enhanced
The stud	ent will create equations that may include, but not limited to: linear, quadratic, cubic, exponential, step and value.	<u>Sample Stems</u>
The stud	ent will solve equations that may include, but not limited to: linear, quadratic, cubic, exponential and absolute	Given the solutions -6, 8, write an absolute value equation that will yield these solutions.
The stud	ent will create equations that may include, but not limited to: linear, quadratic, cubic, exponential, step and value.	Sample answer: x-1 = 7
The stud	ent will solve inequalities that may include, but not limited to: linear, quadratic, cubic, exponential and	Solve $8^{x+6} = 16^{2x+4}$
	ent may use algebraic and/or graphical methods to solve these problems.	Write an absolute value inequality that yields the solution $4 \le x \le 12$
Absolute	Content Limits/Assessment Boundaries e value equations and inequalities should contain no higher degree variable than one (e.g5 x-4 +2 = -20).	Calculator Designation NEUTRAL — a calculator may or
7.250141	Table equalities and inequalities on and contain no inglief defice variable than one (e.g. 5/x 4/ 2 = 20).	may not be available for items

-6-7	Mathematics	A2.REI.A.2
DEI		AZ.ILLI.A.Z
REI	Reasoning with Equations and Inequalities	
Α	Solve equations and inequalities.	
2	Solve rational equations where numerators and denominators are polynomials, and where extraneous solutions	s may result.
	Expectation Unwrapped	DOK Ceiling
ho stus	ant will salve rational equations by various mathods including instances when the numerator and denominator	2
	ent will solve rational equations by various methods, including instances when the numerator and denominator nomials.	Item Format
re pory	iorniais.	Selected Response
he stud	ent will check solutions and identify those that are extraneous.	Constructed Response
		Technology Enhanced
		Sample Stems
	Content Limits/Assessment Boundaries	Calculator Designation
_	egree polynomials should be factorable and not exceed degree three.	NEUTRAL – a calculator may or
ll coeff	cients should be integers.	may not be available for items

	Mathematics	A2.REI.B.3
REI	Reasoning with Equations and Inequalities	
В	Solve general systems of equations and inequalities.	
3	Create and solve systems of equations that may include non-linear equations and inequalities.	
	Expectation Unwrapped	DOK Ceiling
The stud	ent will write a system of equations to model a context or setting that may include non-linear equations and	Item Format
inequalit	ies.	Selected Response
The stud	ent will solve systems of equations that may include non-linear equations and inequalities.	Constructed Response
		Technology Enhanced
		Sample Stems
	Content Limits/Assessment Boundaries	Calculator Designation
Systems	of equations should be limited to: linear – linear – linear, linear – quadratic and quadratic – quadratic.	YES – a calculator will be available
	of equations should only have only three or less unknowns.	for items

	Mathematics	A2.APR.A.1
APR	Arithmetic with Polynomials and Rational Expressions	
Α	Perform operations on polynomials and rational expressions.	
1	Extend the knowledge of factoring to include factors with complex coefficients.	
The stud	Expectation Unwrapped ent will extend the knowledge of factoring to completely factor general polynomial expressions.	DOK Ceiling 2
	The lent will factor simple expressions that require complex coefficients such as, $x^2 + 16 = (x + 4i)(x - 4i)$.	Selected Response Constructed Response Technology Enhanced Sample Stems Factor $x^3 + 8$ Factor completely $2x^4 + 250x$ $4x^4 - x^3 - 8x + 2$ $x^4 + 3x^3 - 4x^2 - 12x$
cubes, G	Content Limits/Assessment Boundaries ne following factoring problems can be assessed: difference of squares, trinomials, sum of cubes, difference of CF, factor by grouping and quartic with no more than four terms. g with complex coefficients should be limited to the sum of squares.	Calculator Designation NEUTRAL – a calculator may or may not be available for items

	Mathematics	A2.APR.A.2
APR	Arithmetic with Polynomials and Rational Expressions	
Α	Perform operations on polynomials and rational expressions.	
2	Understand the Remainder Theorem and use it to solve problems.	
	Expectation Unwrapped	DOK Ceiling
The stud	ent will divide polynomials, using long division and synthetic division, by given factors or zeros to determine ctors.	2 Item Format Salacted Regreeses
Students	s will understand that a remainder of zero indicates the divisor is a factor of the dividend.	Selected Response Constructed Response Technology Enhanced
Students	s will understand that a remainder other than zero indicates the divisor is not a factor of the dividend.	Sample Stems
Students	s will express the result as a quotient with a remainder.	
	Content Limits/Assessment Boundaries should not be greater than degree two. Is should not be greater than degree four.	Calculator Designation NEUTRAL – a calculator may or may not be available for items

	Mathematics	A2.APR.A.3
APR	Arithmetic with Polynomials and Rational Expressions	
Α	Perform operations on polynomials and rational expressions.	
3	Find the least common multiple of two or more polynomials.	
The stud	Expectation Unwrapped lent will determine the least common multiple for two or more polynomials.	DOK Ceiling 1 Item Format Selected Response Constructed Response Technology Enhanced Sample Stems
Use only	Content Limits/Assessment Boundaries factorable polynomials of degree four or less.	Calculator Designation NEUTRAL — a calculator may or may not be available for items

	Mathematics	A2.APR.A.4
APR	Arithmetic with Polynomials and Rational Expressions	
Α	Perform operations on polynomials and rational expressions.	
4	Add, subtract, multiply and divide rational expressions.	
	Expectation Unwrapped	DOK Ceiling
	ent will add and subtract rational expressions, including those with polynomial numerators and denominators, those with unlike denominators.	2 Item Format Selected Response
The stud	ent will multiply and divide rational expressions, including those with polynomial numerators and ators.	Constructed Response Technology Enhanced
Final ans	wers should not have common factors in the numerators and denominators.	Sample Stems
•	Content Limits/Assessment Boundaries ials should not exceed degree four.	<u>Calculator Designation</u> NEUTRAL – a calculator may or
The num	ber of expressions should not exceed three for an addition, subtraction or multiplication problem.	may not be available for items

High School Algebra 2		
	Mathematics	A2.APR.A.5
APR	Arithmetic with Polynomials and Rational Expressions	
Α	Perform operations on polynomials and rational expressions.	
5	Identify zeros of polynomials when suitable factorizations are available, and use the zeros to sketch the functio	n defined by the polynomial.
		T
	Expectation Unwrapped	DOK Ceiling
The stud	ent will factor polynomials and use the zero product property to identify the zeros.	3
		Item Format Selected Response
	ent will use the zeros and other key characteristics to sketch the function defined by the polynomial (x- and y-	Constructed Response
intercep	rs, end behavior, local minima and maxima).	Technology Enhanced
		Sample Stems
	Content Limits/Assessment Boundaries	Calculator Designation
Polynom	ials should be of no greater degree than four.	NEUTRAL – a calculator may or
•		may not be available for items

	Mathematics	A2.IF.A.1
IF	Interpreting Functions	71200000
A	Use and interpret functions.	
1	Identify and interpret key characteristics of functions represented graphically with tables, and with algebraic sy	mholism to solve problems
_	indentity and interpret her districtions of functions represented graphically with tables, and with algebraic sy	moons in to some problems.
	Expectation Unwrapped	DOK Ceiling
	ent will identify the following key characteristics of functions from graphs, tables and equations: domain,	Item Format
	nd behavior, x- and y-intercepts, local maxima and minima values, symmetries, points of discontinuity, intervals	Selected Response
or increa	sing and decreasing, and horizontal and vertical asymptotes.	Constructed Response
The stud	ent will identify these key characteristics for general polynomials: square roots, cube roots, absolute value of	Technology Enhanced
linear fu	nctions, simple piece-wise defined, step functions, exponential, logarithmic and rational functions.	Sample Stems
The estimate		
The stud	ent will be able to represent a given function as a table, equation or graph.	
The stud	ent will be able to determine specific values of a function from a table, graph or equation.	
	Content Limits/Assessment Boundaries	Calculator Designation
	ials should be of no greater degree than four. ts are ordered pairs.	YES – a calculator will be available for items
	is are ordered pairs. Ional functions to those without oblique asymptotes.	ioi itellis

nigh School Algebra Z		
	Mathematics	A2.IF.A.2
IF	Interpreting Functions	
Α	Use and interpret functions.	
2	Translate between equivalent forms of functions.	
	Expectation Unwrapped	DOK Ceiling
		2
The stuc	ent will translate between equivalent forms of functions.	Item Format
The stuc	ent will find equivalent forms of functions to highlight key characteristics.	Selected Response
THE State	che will find equivalent forms of functions to highlight key characteristics.	Constructed Response
The stud	ent will write a quadratic function in vertex form, standard form and/or in intercept form by factorization,	Technology Enhanced
complet	ing the square and multiplication.	Sample Stems
	Content Limits/Assessment Boundaries	Calculator Designation
Polynom	ials should not exceed degree four.	NEUTRAL – a calculator may or
. 5.,511		may not be available for items

ingii s	cnool Algebra 2	
	Mathematics	A2.BF.A.1
BF	Building Functions	
Α	Create new functions from existing functions.	
1	Create new functions by applying the four arithmetic operations and composition of functions (modifying the	domain and range as necessary).
	Expectation Unwrapped	DOK Ceiling
The stud	ant will add functions to create now functions and determine the domain and range of the new function	2
	ent will add functions to create new functions and determine the domain and range of the new function ng the domain and range as necessary).	Item Format
(mouny)	is the domain and range as necessary).	Selected Response
The stud	ent will subtract functions to create new functions and determine the domain and range of the new function	Constructed Response
(modifyii	ng the domain and range as necessary).	Technology Enhanced
		Sample Stems
	ent will multiply functions to create new functions and determine the domain and range of the new function	
(modifyii	ng the domain and range as necessary).	
The stud	ent will divide functions to create new function, and determine the domain and range of the new function	
	ng the domain and range as necessary).	
The stud	ent will compose functions and determine the domain and range of the new function.	
	Content Limits/Assessment Boundaries	Calculator Designation
The num	ber of functions to compose should be restricted to two.	NEUTRAL – a calculator may or
	ee of the polynomials to be composed should be no greater than a linear function with a quadratic function.	may not be available for items
]		

	Mathematics	A2.BF.A.2
BF	Building Functions	
Α	Create new functions from existing functions.	
2	Derive inverses of functions and compose the inverse with the original function to show that the function	ons are inverses.
	Expectation Unwrapped	DOK Ceiling
ho stu	dent will derive inverses of given functions	2
ne stu	dent will derive inverses of given functions.	Item Format
he stu	dent will compose functions to determine if they are inverses.	Selected Response
	·	Constructed Response
The stu	dent will compose the inverse with the original function to prove that the functions are inverses.	Technology Enhanced
		Sample Stems
	Content Limits/Assessment Boundaries	Calculator Designation
he deg	ree of functions for this standard should not be greater than four.	YES – a calculator will be available
		for items

High 3	ocnool Algebra 2	
	Mathematics	A2.BF.A.3
BF A 3	Building Functions Create new functions from existing functions. Describe the effects of transformations algebraically and graphically; create vertical and horizontal translations, and dilations (expansions/compressions) for a variety of functions (linear, quadratic, cubic, square and cube roo logarithmic).	
The stud (expansion to the stud cubic, square to the stud logarithm	ent will describe the effects of transformations algebraically using <i>a</i> , <i>h</i> , and <i>k</i> , given an equation in the form <i>h</i>)+ <i>k</i> , or given other general forms of the functions listed. ent will describe the effects of transformations graphically using terms such as horizontal or vertical stretch on), or shrink (compression), reflection, horizontal and vertical translation and dilation. ent will create equations from the parent functions that produce a variety of transformations (linear, quadratic, uare and cube root, absolute value, exponential, and logarithmic). ent will create graphs from the (linear, quadratic, cubic, square and cube root, absolute value, exponential, and nic) parent graphs that demonstrate vertical stretch (expansion), or shrink (compression), reflection, horizontal ical translation and dilation.	DOK Ceiling 3 Item Format Selected Response Constructed Response Technology Enhanced Sample Stems
	Content Limits/Assessment Boundaries lues of $-3 \le a \le 3$. d k values of $-10 \le h \le 10$ and $-10 \le k \le 10$.	Calculator Designation NEUTRAL – a calculator may or may not be available for items

	Mathematics	A2.FM.A.1
FM	Modeling	
Α	Use functions to model real-world problems.	
1	Create functions and use them to solve applications of quadratic and exponential function model problems.	
	Expectation Unwrapped	DOK Ceiling 3
The stud	dent will create quadratic or exponential equations to model problems.	Item Format
graphica	dent will solve quadratic or exponential equations to determine solutions to problems algebraically or ally (e.g. price-demand-cost-revenue-profit situations, compound interest problems and exponential growth or roblems).	Selected Response Constructed Response Technology Enhanced
		Sample Stems
	Content Limits/Assessment Boundaries	Calculator Designation YES – a calculator will be available for items

	Mathematics	A2.DS.A.1
DS	Data and Statistical Analysis	
Α	Make inferences and justify conclusions.	
1	Analyze how random sampling could be used to make inferences about population parameters.	
	Expectation Unwrapped	DOK Ceiling
The stud	dent will understand random sampling.	3
	dent will explain how a random sample can be used to make an inference about a population.	Item Format Selected Response Constructed Response
The stud	dent will analyze situations to determine if random sampling was used.	Technology Enhanced
		Sample Stems
	Content Limits/Assessment Boundaries	<u>Calculator Designation</u>
		NEUTRAL – a calculator may or may not be available for items

tails in a row cause you to que the model? Content Limits/Assessment Boundaries Calculator Designation		Mathematics Mathematics	A2.DS.A.2
Expectation Unwrapped The student will determine whether a specified model is consistent with a given data set. Expectation Unwrapped The student will determine whether a specified model is consistent with a given data set. Expectation Unwrapped Item Format Selected Response Constructed Response Technology Enhanced Sample Stems A model says a spinning coin heads up with probability 0.5. Would an experimental result tails in a row cause you to que the model? Content Limits/Assessment Boundaries Content Limits/Assessment Boundaries Calculator Designation NEUTRAL – a calculator may	DS	Data and Statistical Analysis	
Expectation Unwrapped The student will determine whether a specified model is consistent with a given data set. DOK Ceiling 2 Item Format Selected Response Constructed Response Technology Enhanced	Α	Make inferences and justify conclusions.	
The student will determine whether a specified model is consistent with a given data set. The student will determine whether a specified model is consistent with a given data set. The student will determine whether a specified model is consistent with a given data set. The student will determine whether a specified model is consistent with a given data set. The student will determine whether a specified model is consistent with a given data set. The student will determine whether a specified model is consistent with a given data set. The student will determine whether a specified model is consistent with a given data set. The student will determine whether a specified model is consistent with a given data set. The student will determine whether a specified model is consistent with a given data set. The student will determine whether a specified model is consistent with a given data set. The student will determine whether a specified model is consistent with a given data set. The student will determine whether a specified mean set. The student will determine whether a specified mean set of the s	2	Determine whether a specified model is consistent with a given data set.	
The student will determine whether a specified model is consistent with a given data set. Item Format		Expectation Unwrapped	
Selected Response Constructed Response Technology Enhanced Sample Stems A model says a spinning coin heads up with probability 0.5. Would an experimental result tails in a row cause you to que the model? Content Limits/Assessment Boundaries Content Limits/Assessment Boundaries Calculator Designation NEUTRAL — a calculator may	The stud	ent will determine whether a specified model is consistent with a given data set	2
Constructed Response Technology Enhanced Sample Stems A model says a spinning coin theads up with probability 0.5. Would an experimental result tails in a row cause you to quet the model? Content Limits/Assessment Boundaries Content Limits/Assessment Boundaries Calculator Designation NEUTRAL — a calculator may	The state	ent will determine whether a specified model is consistent with a given data set.	
Technology Enhanced Sample Stems A model says a spinning coin theads up with probability 0.5. Would an experimental result tails in a row cause you to quet the model? Content Limits/Assessment Boundaries Calculator Designation NEUTRAL – a calculator may			
Sample Stems A model says a spinning coin theads up with probability 0.5. Would an experimental result tails in a row cause you to quethe model? Content Limits/Assessment Boundaries Calculator Designation NEUTRAL — a calculator may			·
A model says a spinning coin heads up with probability 0.5. Would an experimental result tails in a row cause you to que the model? Content Limits/Assessment Boundaries Calculator Designation NEUTRAL — a calculator may			Technology Enhanced
heads up with probability 0.5. Would an experimental result tails in a row cause you to que the model? Content Limits/Assessment Boundaries Calculator Designation NEUTRAL — a calculator may			Sample Stems
heads up with probability 0.5. Would an experimental result tails in a row cause you to que the model? Content Limits/Assessment Boundaries Calculator Designation NEUTRAL — a calculator may			A model says a spinning coin falls
Would an experimental result tails in a row cause you to que the model? Content Limits/Assessment Boundaries Calculator Designation NEUTRAL — a calculator may			
tails in a row cause you to que the model? Content Limits/Assessment Boundaries Calculator Designation NEUTRAL — a calculator may			Would an experimental result of 5
Content Limits/Assessment Boundaries Calculator Designation NEUTRAL – a calculator may			tails in a row cause you to question
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·		Content Limits/Assessment Boundaries	<u>Calculator Designation</u>
Specified models might include dot plots, histograms, frequency tables, lists or simulation result statements. may not be available for items may not be available for items			NEUTRAL – a calculator may or
	Specifie	models might include dot plots, histograms, frequency tables, lists or simulation result statements.	may not be available for items

	Mathematics	A2.DS.A.3
DS	Data and Statistical Analysis	
Α	Make inferences and justify conclusions.	
3	Describe and explain the purposes, relationship to randomization and differences among sample surveys, exp	periments and observational studies.
	Expectation Unwrapped	DOK Ceiling
The stud	lent will describe and explain the purpose and relationship to random sampling in sample surveys.	<u>Item Format</u>
The stud	lent will describe and explain the purpose and relationship to randomization of applying treatment in ents.	Selected Response Constructed Response Technology Enhanced
The studies.	lent will describe and explain the purpose and relationship to randomization in sampling for observational	Sample Stems
	lent will describe and explain the differences between random samples in surveys, experiments and tional study.	
	Content Limits/Assessment Boundaries	Calculator Designation NEUTRAL — a calculator may or may not be available for items

	Mathematics	A2.DS.A.4
DS	Data and Statistical Analysis	
Α	Make inferences and justify conclusions.	
4	Use data from a sample to estimate characteristics of the population and recognize the meaning of the	e margin of error in these estimates.
	Expectation Unwrapped	DOK Ceiling
he stud	dent will use data from a sample to estimate characteristics of the population.	2
		<u>Item Format</u>
he stud	dent will recognize the meaning of margin of error(given a margin of error) in the estimates.	Selected Response
		Constructed Response
		Technology Enhanced
		Sample Stems
		Marvin's Chip Company claims
		their chip bags contain a mean of
		oz of chips with a margin of error +/04 oz.
		A randomly selected box containing
		10 bags of chips is selected and th
		individual bags are weighed with
		the following results (in oz):
		9.0 9.3 8.5 8.8 9.1 9.5 8.9 8.8
		9.2 8.9
		Does the data support Marvin's
		claim?
	Content Limits/Assessment Boundaries	Calculator Designation
ata sar	mples should be limited to ten. Decimal values should be no more than three places.	YES – a calculator will be available
		for items

DS A Make inferences and justify conclusions. Describe and explain how the relative sizes of a sample and the population affect the margin of error of predictions. Expectation Unwrapped The student will be able to explain that larger sample sizes lead to a smaller margin of error. The students will be able to explain that larger populations require a larger sample size to decrease the margin of error. The students will be able to describe how the validity of inference is affected by the margin of error.	2.DS.A.5
Make inferences and justify conclusions. Describe and explain how the relative sizes of a sample and the population affect the margin of error of predictions. Expectation Unwrapped The student will be able to explain that larger sample sizes lead to a smaller margin of error. The student will be able to explain that larger populations require a larger sample size to decrease the margin of error. The students will be able to describe how the validity of inference is affected by the margin of error.	
Describe and explain how the relative sizes of a sample and the population affect the margin of error of predictions. Expectation Unwrapped The student will be able to explain that larger sample sizes lead to a smaller margin of error. Ite Selected Resp Constructed R The students will be able to describe how the validity of inference is affected by the margin of error.	
Expectation Unwrapped The student will be able to explain that larger sample sizes lead to a smaller margin of error. The student will be able to explain that larger populations require a larger sample size to decrease the margin of error. The students will be able to describe how the validity of inference is affected by the margin of error. Expectation Unwrapped Selected Resp. Constructed Resp. Technology En	
The student will be able to explain that larger sample sizes lead to a smaller margin of error. The student will be able to explain that larger populations require a larger sample size to decrease the margin of error. The students will be able to describe how the validity of inference is affected by the margin of error. Technology Error.	
The student will be able to explain that larger sample sizes lead to a smaller margin of error. The student will be able to explain that larger populations require a larger sample size to decrease the margin of error. The students will be able to describe how the validity of inference is affected by the margin of error. Technology Error.	
The student will be able to explain that larger sample sizes lead to a smaller margin of error. The student will be able to explain that larger populations require a larger sample size to decrease the margin of error. The students will be able to describe how the validity of inference is affected by the margin of error. Technology En	OK Ceiling
The student will be able to explain that larger populations require a larger sample size to decrease the margin of error. The students will be able to describe how the validity of inference is affected by the margin of error. Selected Resp Constructed R Technology Error.	2
The student will be able to explain that larger populations require a larger sample size to decrease the margin of error. Selected Resp Constructed R Technology Er	em Format
The students will be able to describe how the validity of inference is affected by the margin of error. Constructed R Technology Er	
The students will be able to describe now the validity of inference is affected by the margin of error.	•
Sar	ıhanced
	nple Stems
Content Limits/Assessment Boundaries Calcula	tor Designation
	calculator may or
may not be av	ailable for items

DS Make inferences and justify conclusions. Analyze decisions and strategies using probability concepts. Expectation Unwrapped Dok Ceiling	.DS.A.6	A2.DS.A.6	Mathematics	
Make inferences and justify conclusions. Analyze decisions and strategies using probability concepts. Expectation Unwrapped Butter Form: Selected Response Constructed Response Technology Enhanced Swhite marble, you che marble from the bag we looking, put it aside an choose another marble without looking. From the list below, semethods that would redetermining the probawould select one red a marble. Content Limits/Assessment Boundaries Calculator will Calculator Designation Calculator will Cal	.231110	712.55.7110		DS
Expectation Unwrapped The student will analyze decisions using probability concepts. The student will analyze strategies using probability concepts. The student will analyze strategies using probability concepts. The student will analyze strategies using probability concepts. Selected Response Constructed Response Technology Enhanced Sample Ster Given a bag with 5 red 5 white marble, you che marble from the bag we looking, put it aside an choose another marble without looking. From the list below, se methods that would redetermining the proba would select one red a marble. Content Limits/Assessment Boundaries Calculator Desig YES – a calculator will a calculat			·	
Expectation Unwrapped The student will analyze decisions using probability concepts. The student will analyze strategies using probability concepts. The student will analyze strategies using probability concepts. Selected Response Constructed Response Technology Enhanced Sample Ster Given a bag with 5 red 5 white marble, you che marble from the bag we looking, put it aside an choose another marble without looking. From the list below, se methods that would redetermining the proba would select one red a marble. Content Limits/Assessment Boundaries Calculator Desig YES – a calculator will a c				
The student will analyze decisions using probability concepts. The student will analyze strategies using probability concepts. The student will analyze strategies using probability concepts. Selected Response Constructed Response Technology Enhanced Sample Ster Given a bag with 5 red 5 white marble, you ch marble from the bag w looking, put it aside an choose another marble without looking. From the list below, se methods that would re determining the proba would select one red a marble. Content Limits/Assessment Boundaries Calculator Desig YES – a calculator will it.			, many to desire and on a together	
The student will analyze decisions using probability concepts. The student will analyze strategies using probability concepts. Selected Response Constructed Response Technology Enhanced Sample Ster Given a bag with 5 red 5 white marble, you che marble from the bag we looking, put it aside an choose another marble without looking. From the list below, see methods that would redetermining the proba would select one red a marble. Content Limits/Assessment Boundaries Content Limits/Assessment Boundaries Calculator Designation and the probability of the p	K Ceiling	DOK Ceiling	Expectation Unwrapped	
The student will analyze strategies using probability concepts. Selected Response Constructed Response Technology Enhanced Given a bag with 5 red 5 white marble, you ch marble from the bag w looking, put it aside an choose another marble without looking. From the list below, se methods that would re determining the proba would select one red a marble. Content Limits/Assessment Boundaries Calculator Desig YES – a calculator will I	_	_		
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Given a bag with 5 red 5 white marble, you che marble from the bag we looking, put it aside an choose another marble without looking. From the list below, see methods that would redetermining the probate would select one red a marble. Content Limits/Assessment Boundaries Calculator Designation Calculator Designation Calculator VESI Calculator VESI YESI Calculator Will II	nanced	Technology Enhanced		
5 white marble, you che marble from the bag we looking, put it aside an choose another marble without looking. From the list below, see methods that would redetermining the probate would select one red at marble. Content Limits/Assessment Boundaries Calculator Design YES — a calculator will less than the beginning the probate would select one reduction.	ple Stems	Sample Stems		
marble from the bag w looking, put it aside an choose another marble without looking. From the list below, se methods that would re determining the proba would select one red a marble. Content Limits/Assessment Boundaries Calculator Designation Calculator Version Calculator Version YES — a calculator will be		Given a bag with 5 red marb		
looking, put it aside an choose another marble without looking. From the list below, se methods that would re determining the proba would select one red a marble. Content Limits/Assessment Boundaries Calculator Design		5 white marble, you choose		
choose another marble without looking. From the list below, se methods that would redetermining the probation would select one red a marble. Content Limits/Assessment Boundaries Calculator Designation (Content Limits/Assessment Boundaries) Calculator Designation (Content Limits/Assessment Boundaries)				
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		YES – a calculator will be ava	Content Limits/Assessment boundaries	

	Mathematics	A2.DS.A.7
DS	Data and Statistical Analysis	
Α	Make inferences and justify conclusions.	
7	Evaluate reports based on data.	
The stud	Expectation Unwrapped dent will evaluate statistical reports to determine identify statistical issues such as bias, validity of resource, ble reporting of statistical analysis and accurate graphical representations.	DOK Ceiling 3 Item Format Selected Response Constructed Response Technology Enhanced Sample Stems
	Content Limits/Assessment Boundaries	Calculator Designation YES – a calculator will be available for items

High School Algebra 2			
	Mathematics	A2.DS.B.8	
DS	Data and Statistical Analysis		
В	Fit a data set to a normal distribution.		
8	Know and use the characteristics of normally distributed data sets; predict what percentage of the data will be multiple of standard deviations above or below the mean.	above or below a given value that is a	
	Expectation Unwrapped	DOK Ceiling	
	ent will know and be able to use the 68-95-99.7 rule to determine the percentages of data above or below the given standard deviations.	3 <u>Item Format</u>	
		Selected Response	
	ent will be able to draw and label the normal curve with values on the horizontal axis (when given the mean dard deviation).	Constructed Response Technology Enhanced	
The student will be able to draw and label the standard normal curve with percentages using the empirical rule (68-95-99.7 rule).		Sample Stems Suppose the test scores in a school are normally distributed with a mean of 72 and a standard	
3 2 1 0 1 2 3 Standard Deviations		deviation of 8. Find what percentage of the students scored above 64. A student takes a simple random sample of students from his high school of 2580 students asking how much they usually spend on fast food each week. The data was normally distributed with a mean of \$6.50 and a standard deviation of \$1.75. Approximately how many students at the school spend between \$8.25 and \$10 each week?	
	Content Limits/Assessment Boundaries	<u>Calculator Designation</u>	
Standard	deviations should be restricted to integer values from negative three to three.	YES – a calculator will be available for items	

	Mathematics	A2.DS.B.9
DS	Data and Statistical Analysis	
В	Fit a data set to a normal distribution.	
9	Fit a data set to a distribution using its mean and standard deviation to determine whether the data is approxin	nately normally distributed.
	Expectation Unwrapped	DOK Ceiling
mean, if	lent will determine from a data set if approximately 68% of the data is within one standard deviation of the approximately 95% of the data is within two standard deviations of the mean, and if approximately 99.7% (all) ata is within three standard deviations of the mean.	Item Format Selected Response Constructed Response Technology Enhanced Sample Stems
Data set	Content Limits/Assessment Boundaries s should be no more than fifty numbers.	Calculator Designation YES – a calculator will be available for items