

2-1 Unit Rates with complex Fractions

Complex Fractions

A fraction within a fraction!

Ex 1)

$$\frac{\frac{4}{5}}{\frac{2}{3}}$$

$$\frac{5}{5} \cdot \frac{3}{3}$$

$$\cdot \frac{3}{2}$$

$$\frac{3}{2}$$

$$\frac{12}{10}$$

$$\frac{5}{4}$$

$$\cdot$$

$$\frac{3}{2}$$

$$=$$

$$\frac{12}{10}$$

Ex 2)

$$\frac{\frac{1}{2}}{\frac{4}{5}} = \frac{1}{2} \div \frac{4}{5}$$

$$\frac{1}{2} \cdot \frac{5}{4}$$

$$\frac{5}{8}$$

$$\frac{3}{2} \rightarrow \frac{5}{4}$$

$$\frac{5}{4}$$

$$\frac{15}{8}$$

$$\frac{15}{8}$$

Unit Rates!

If I drive 300 miles in 4 hours, what is my rate of speed (miles per hour)?

$$300 \text{ mil} / 4 \text{ hrs} = 75 \text{ mil/hr.}$$

If I picked $5 \frac{1}{2}$ pounds of apples in $\frac{3}{4}$ hour, how many pounds per hour did I pick?

$$5 \frac{1}{2} \text{ lbs} / \frac{3}{4} \text{ hr}$$

$$\frac{5 \frac{1}{2}}{\frac{3}{4}} = 5 \frac{1}{2} \div \frac{3}{4} \quad 7 \frac{1}{3} \text{ lbs/hr}$$

$$\begin{array}{r} 6 \overline{)44} \\ \underline{42} \\ 2 \end{array}$$

$$\begin{array}{r} 11 \\ \downarrow \\ 2 \overline{)22} \\ \underline{20} \\ 2 \end{array} \quad \begin{array}{r} 3 \\ \overline{)4} \\ \underline{3} \\ 1 \end{array} \quad \begin{array}{r} 7 \frac{1}{3} \text{ lbs/hr} \\ \uparrow \\ 7 \frac{2}{6} \end{array}$$

$$\frac{11}{2} \cdot \frac{4}{3} = \frac{44}{6}$$

Team:

Lexi walks $3\frac{1}{2}$ miles in $1\frac{1}{4}$ hours. How many miles per hour does she walk?

$$3\frac{1}{2} \text{ mil} / 1\frac{1}{4} \text{ hrs}$$

$$3\frac{1}{2} \div 1\frac{1}{4}$$

$$\frac{7}{2} \div \frac{5}{4} =$$

$$\frac{7}{2} \rightarrow \frac{4}{5} = \frac{28}{10}$$

$$\begin{array}{r} 10 \overline{) 28} \\ \underline{20} \\ 8 \end{array}$$

$$2\frac{8}{10}$$

$$2\frac{4}{5} \text{ mil/hr}$$

~~Pair~~

I can read $\frac{3}{4}$ of a page in $\frac{2}{3}$ of a minute.
 How many pages per minute can I read?

$$\frac{3}{4} \div \frac{2}{3}$$

K S F

$$\frac{3}{4} \cdot \frac{3}{2} = \frac{9}{8} =$$

$$\frac{1}{8} \left| \frac{9}{8} \right.$$

(Note: The fraction $\frac{9}{8}$ inside the division symbol is heavily scribbled out.)

$$1 \frac{1}{8} \text{ pages/min}$$

p/min

~~Solo:~~

I use $\frac{4}{5}$ cup of tomato sauce when I cut my recipe in $\frac{1}{2}$. How many cups per recipe are there?

~~$\frac{4}{5}$ cup~~ $\frac{1}{2}$ recipe

$$\frac{4}{5} \div \frac{1}{2}$$

K S F

$$\frac{4}{5} \cdot \frac{2}{1} = \frac{8}{5} = 1\frac{3}{5}$$

cups/
recipe

$$\begin{array}{r} 1 \\ 5 \overline{) 5} \\ \underline{5} \\ 0 \end{array}$$

~~$\frac{4}{5} \div \frac{1}{2}$~~

Sometimes we can find unit rates by filling out tables.

Luke likes running. He runs $2\frac{1}{2}$ miles every $\frac{1}{2}$ hour. Complete the table to find out how far he runs in each time interval. Which one shows his unit rate (miles per hour)?

| | | | | | |
|-----------|----------------|---|----------------|----|-----------------|
| Distance | $2\frac{1}{2}$ | 5 | $7\frac{1}{2}$ | 10 | $12\frac{1}{2}$ |
| Time (hr) | $\frac{1}{2}$ | 1 | $1\frac{1}{2}$ | 2 | $2\frac{1}{2}$ |

$5\text{ mil}/1\text{ hr}$

Complete the table to find the unit rate.

Jeff hikes $\frac{1}{2}$ mile every $\frac{1}{4}$ hour. What is his unit rate?

$2 \text{ mil} / \text{hr}$

| | | | | |
|----------|---------------|---------------|---------------|---|
| Distance | $\frac{1}{2}$ | 1 | $\frac{1}{2}$ | 2 |
| Time | $\frac{1}{4}$ | $\frac{1}{2}$ | $\frac{3}{4}$ | 1 |

$$\frac{1}{4} + \frac{1}{4} = \frac{2}{4} = \frac{1}{2}$$

$$\frac{2}{4} + \frac{1}{4} = \frac{3}{4}$$

$$\frac{3}{4} + \frac{1}{4} = \frac{4}{4} = 1$$

Complete the table to find the unit rate.

Lisa hikes $\frac{1}{3}$ mile every $\frac{1}{6}$ hour. What is her unit rate?

| | | | | | | |
|----------|---------------|---------------|---------------|----------------|----------------|---|
| Distance | $\frac{1}{3}$ | $\frac{2}{3}$ | 1 | $1\frac{1}{3}$ | $1\frac{2}{3}$ | 2 |
| Time | $\frac{1}{6}$ | $\frac{1}{3}$ | $\frac{1}{2}$ | $\frac{2}{3}$ | $\frac{5}{6}$ | 1 |

$$\frac{1}{3} + \frac{1}{3} = \frac{2}{3} \quad \left(\frac{2}{3} + \frac{1}{3} = \frac{3}{3} = 1 \right) \quad \frac{3}{3} + \frac{1}{3} = \frac{4}{3} \quad \frac{4}{3} + \frac{1}{3} = \frac{5}{3} = 1\frac{2}{3} \quad \frac{5}{3} + \frac{1}{3} = \frac{6}{3} = 2$$

$$\frac{1}{6} + \frac{1}{6} = \frac{2}{6} = \frac{1}{3} \quad \frac{2}{6} + \frac{1}{6} = \frac{3}{6} = \frac{1}{2} \quad \frac{3}{6} + \frac{1}{6} = \frac{4}{6} = \frac{2}{3} \quad \frac{4}{6} + \frac{1}{6} = \frac{5}{6} \quad \frac{5}{6} + \frac{1}{6} = \frac{6}{6} = 1$$

$2 \text{ mil} / 1 \text{ hr}$

How can we find unit rates?

table OR divide

Which way is easier?

Divide!

Which one is cheaper??? (Find the cost per hour)



Can talk for 1/2 hour

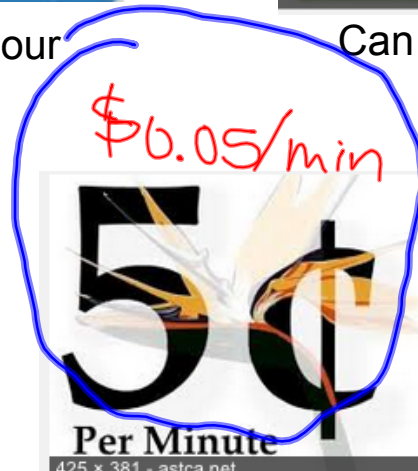
$\$3.25 / \frac{1}{2} \text{ hr}$
 $\$3.25 / 30 \text{ min}$
 $0.1083 \dots$
 $\$0.11 / \text{min}$



Can talk for 2.5 hours

$\$10 / 2.5 \text{ hrs}$
 $\$10 / 150 \text{ min}$
 $0.0666 \dots$
 $\$0.07 / \text{min}$

30
 60
 $+60$
 $\hline 150$
 150 min



$\$0.05 / \text{min}$

